Planning

- Introduction
 - Planning vs. Problem-Solving
 - Representation in Planning Systems
- Situation Calculus
 - The Frame Problem
- STRIPS representation language
 - Blocks World
- Planning with State-Space Search
 - Progression Algorithms
 - Regression Algorithms
- Planning with Plan-Space Search
 - Partial-Order Planning
 - The Plan Graph and GraphPlan
 - SatPlan

Material from Russell & Norvig, chapters 10.3. and 11

Slides based on Slides by Russell/Norvig, Lise Getoor and Tom Lenaerts

Sussman Anomaly

Famous example that shows that subgoals are not independent



goal: on (A, B), on (B, C)

- achieve on (B, C) first:
 - shortest solution will just put B on top of $C \rightarrow$ subgoal has to be undone in order to complete the goal
- achieve on (A, B) first:
 - shortest solution will not put B on $C \rightarrow$ subgoal has do be undone later in order to complete the goal

Partial-Order Planning (POP)

- Progression and regression planning are totally ordered plan search forms
 - this means that in all searched plans the sequence of actions is completely ordered
 - Decisions must be made on how to sequence actions in all the subproblems
 - \rightarrow They cannot take advantage of problem decomposition
- If actions do not interfere with each other, they could be made in any order (or in parallel) → partially ordered plan
 - if a plan for each subgoal only makes minimal commitments to orders
 - only orders those actions that must be ordered for a successful completion of the plan
 - it can re-order steps later on (when subplans are combined)
 - Least commitment strategy:
 - Delay choice during search

Shoe Example

Initial State: nil Goal State: RightShoeOn & LeftShoeOn

```
Action (LeftSock,

PRECOND: -

ADD: LeftSockOn

DELETE: -
```

```
Action(LeftShoe,
PRECOND: LeftSockOn
ADD: LeftShoeOn
DELETE: -
```

```
Action(RightSock,

PRECOND: -

ADD: RightSockOn

DELETE: -
```

Action(RightShoe, PRECOND: RightSockOn ADD: RightShoeOn DELETE: -

Shoe Example

- Total-Order Planner
 - all actions are completely ordered



- Partial-Order Planner
 - may leave the order of some actions undetermined
 - any order is valid



State-Space vs. Plan-Space Search

State-Space Plannning

 Search goes through possible states

Plan-Space Planning

 Search goes through possible plans



POP as a Search Problem

- A solution can be found by a search through Plan-Space:
 - States are (mostly unfinished) plans

Each plan has 4 components:

- A set of actions (steps of the plan)
- A set of ordering constraints: A < B (A before B)</p>
 - Cycles represent contradictions.
- A set of causal links $A \rightarrow p \rightarrow B$ (A adds p for B)
 - The plan may not be extended by adding a new action C that conflicts with the causal link.
 - An action C conflicts with causal link $A \rightarrow p \rightarrow B$
 - if the effect of C is $\neg p$ and if C could come after A and before B
- A set of open preconditions
 - Preconditions that are not achieved by action in the plan

Example of Final Plan

- Actions = {RightSock, RightShoe, LeftSock, LeftShoe, Start, Finish}
- Orderings =

 {RightSock < RightShoe;
 LeftSock < LeftShoe}
- Causal Links =

 {RightSock→RightSockOn→RightShoe,
 LeftSock→LeftSockOn→LeftShoe,
 RightShoe→RightShoeOn→Finish,
 LeftShoe→LeftShoeOn→Finish}



Open preconditions = { }

Search through Plan-Space

- Initial State (empty plan):
 - contains only virtual Start and Finish actions
 - ordering constraint Start < Finish</p>
 - no causal links
 - all preconditions in Finish are open
 - these are the original goal
- Successor Function (refining the plan):

generates all consistent successor states

- picks one open precondition p on an action B
- generates one successor plan for every possible consistent way of choosing action that achieves p
- a plan is consistent iff
 - there are <u>no cycles</u> in the ordering constraints
 - no conflicts with the causal links
- Goal test (final plan):
 - A consistent plan with no open preconditions is a solution.

Subroutines

- Refining a plan with action A, which achieves p for B:
 - add causal link $A \rightarrow p \rightarrow B$
 - add the ordering constraint A < B
 - add Start < A and A < Finish to the plan (only if A is new)</p>
 - resolve conflicts between
 - new causal link $A \rightarrow p \rightarrow B$ and all existing actions
 - new action A and all existing causal links (only if A is new)
- Resolving a conflict between a causal link $A \rightarrow p \rightarrow B$ and an action C
 - we have a conflict if the effect of C is ¬p and C could come after A and before B
 - \rightarrow resolved by adding the ordering constraints C < A or B < C
 - both refinements are added (two successor plans) if both are consistent

Search through Plan-Space

- Operators on partial plans
 - Add an action to fulfill an open condition
 - Add a causal link
 - Order one step w.r.t another to remove possible conflicts
- Search gradually moves from incomplete/vague plans to complete/correct plans
- Backtrack if an open condition is unachievable or if a conflict is irresolvable
 - pick the next condition to achieve at one of the previous choice points
 - ordering of the conditions is irrelevant for completeness (the same plans will be found), but may be relevant for consistency

Executing Partially Ordered Plans

- Any particular order that is consistent with the ordering constraints is possible
 - A partial order plan is executed by repeatedly choosing any of the possible next actions.
- This flexibility is a benefit in non-cooperative environments.

Initial State:	<pre>at(flat,axle),</pre>
	at(spare,trunk)
Goal State:	at(spare,axle)

```
Action( remove(spare,trunk),
PRECOND: at(spare,trunk)
ADD: at(spare,ground)
DELETE: at(spare,trunk)
```

Action(leave-overnight, PRECOND: -ADD: -DELETE: at(spare,ground), at(spare,axle), at(spare,trunk), at(flat,ground), at(flat,axle)

Here we need a **not**, which is not part of the original STRIPS language!

Action(remove(flat,axle),
PRECOND: at(flat,axle)
ADD: at(flat,ground)
DELETE: at(flat,axle)

- Initial plan:
 - Action start has the current state as effects
 - Action finish has the goal as preconditions



At(Spare,Axle) Finish

- Action putOn (spare, axle) is the only action that achieves the goal at (spare, axle)
- the current plan is refined to one new plan:
 - putOn (spare, axle) is added to the list of actions
 - add constraints putOn(spare,axle) < finish and > start
 - add causal link putOn(spare,axle) → at(spare,axle) → finish
 - the preconditions of putOn(spare,axle) are now open

Att Spara Truph		
Stort Al(Spare, Trunk)	At(Spare, Ground)	Finish
		1 111311
Al(Fial,Axie)	$\neg At(Flat, Axle)$	

- we select the next open precondition at (spare, ground) as a goal
- only remove (spare, trunk) can achieve this goal
- the current plan is refined to a new one as before, causal links are added



- we select the next open precondition not(at(flat,axle)) as a goal
- could be achieved with two actions
 - leave-overnight
 - remove(flat,axle)
 - \rightarrow we have two successor plans



Plan 1: leave-overnight

- is in conflict with the constraint remove (spare, trunk) → at (spare, ground) → putOn (spare, axle)
 - \rightarrow has to be ordered before remove (spare, trunk)
 - cannot be ordered after putOn (spare, axle) because it achieves its precondition
 - constraint leave-overnight < remove(spare,trunk) is added</pre>



Plan 1: leave-overnight

- the condition at (spare, trunk) has to be achieved next
 - start is the only action that can achieve this
 - however, start→at(spare,trunk)→remove(spare,trunk) is in conflict with leave-overnight
 - this conflict cannot be resolved → backtracking



Plan 2: remove (flat, axle)

- achieves goal not(at(flat,axle))
- corresponding causal link and order relation are added
- at(flat,axle) becomes open precondition



- open precondition at (spare, trunk) is selected as goal
 - action start is added
 - corresponding causal link and order relation are added



- open precondition at (spare, trunk) is selected as goal
 - action start is added
 - corresponding causal link and order relation are added
- open precondition at(flat,axle) is selected as goal
 - action start can achieve this and is already part of the plan
 - corresponding causal link and order relation are added
- no more open preconditions remain

 \rightarrow plan is completed



POP in First-Order Logic

- Operators may leave some variables unbound
- Example
 - Achieve goal on (a,b) with action move (a, From, b)
 - It remains unspecified from where block a should be moved (PRECOND: on (a, From))

```
clear(Block),
clear(To),
ADD: on(Block,To),
clear(From),
DELETE: on(Block,From),
clear(To)
```

Action (move (Block, From, To) ,

PRECOND: on (Block, From),

Two approaches

- Decide for one binding and backtrack later on (if necessary)
- Defer the choice for later (least commitment)
- Problems with least commitment:
 - e.g., an action that has on (a, From) on its delete-list will only conflict with above if both are bound to the same variable
 - can be resolved by introducing inequality constraint.

Heuristics for Plan-Space Planning

- Not as well understood as heuristics for state-space planning
- General heuristic: number of distinct open preconditions
 - maybe minus those that match the initial state
 - underestimates costs when several actions are needed to achieve a condition
 - overestimates costs when multiple goals may be achieved with a single action
- Choosing a good precondition to refine has also a strong impact
 - select open condition that can be satisfied in the fewest number of ways
 - analogous to most-constrained variable heuristic from CSP
 - Two important special cases:
 - select a condition that cannot be achieved at all (early failure!)
 - select deterministic conditions that can only be achieved in one way

Planning Graph

- A planning graph is a special structure used to
 - achieve better heuristic estimates.
 - directly extract a solution using GRAPHPLAN algorithm
- Consists of a sequence of levels (time steps in the plan)
 - Level 0 is the initial state.
- Each level consists of a set of literals and a set of actions.
 - Literals = all those that *could* be true at that time step
 - depending on the actions executed at the preceding time step
 - Actions = all those actions that could have their preconditions satisfied at that time step
 - depending on which of the literals actually hold.
 - Only a restricted subset of possible negative interactions among actions is recorded
- Planning graphs work only for propositional problems
 - STRIPS and ADL can be propositionalized

- Initial state: have (cake)
- Goal state: have(cake), eaten(cake)

```
Action( eat(cake),
PRECOND: have(cake)
ADD: eaten(cake)
DELETE: have(cake)
)
```

```
Action(bake(cake),

PRECOND: not(have(cake))

ADD: have(cake)

DELETE: -

)
```

Persistence Actions

- pseudo-actions for which the effect equals the precondition
- analogous to frame axioms
- are automatically added by the planner

Mutual exclusions

 link actions or preconditions that are mutually exclusive (*mutex*)





• Start at level S_0 , determine action level A_0 and next level S_1

- A₀ contains all actions whose preconditions are satisfied in the previous level S₀
- Connect preconditions and effects of these actions
- Inaction is represented by persistence actions
- Level A₀ contains the actions that could occur
 - Conflicts between actions are represented by mutex links



- Per construction, Level S₁ contains all literals that could result from picking any subset of actions in A₀
 - Conflicts between literals that can not occur together are represented by mutex links.
 - S₁ defines multiple possible states and the mutex links are the constraints that hold in this set of states
- Continue until two consecutive levels are identical
 - Or contain the same amount of literals (explanation later)

Mutex Relations

- A mutex relation holds between two actions when:
 - Inconsistent effects:
 - one action negates the effect of another.
 - Interference:
 - one of the effects of one action is the negation of a precondition of the other
 - Competing needs:
 - one of the preconditions of one action is mutually exclusive with the precondition of the other.
- A mutex relation holds between two literals when:
 - Inconsistent support:
 - If one is the negation of the other OR
 - if <u>each</u> possible action pair that could achieve the literals is mutex





Initial State:	<pre>at(flat,axle),</pre>
	at(spare,trunk)
Goal State:	at(spare,axle)

```
Action( remove(spare,trunk),
PRECOND: at(spare,trunk)
ADD: at(spare,ground)
DELETE: at(spare,trunk)
```

Action(leave-overnight, PRECOND: -ADD: -DELETE: at(spare,ground), at(spare,axle), at(spare,trunk), at(flat,ground), at(flat,axle)

Here we need a **not**, which is not part of the original STRIPS language!

Action(remove(flat,axle),
PRECOND: at(flat,axle)
ADD: at(flat,ground)
DELETE: at(flat,axle)

• *S*₀ consist of 5 literals (initial state and the CWA literals)

S₀ At(Spare,Trunk)

At(Flat,Axle)

¬At(Spare,Axle)

¬At(Flat,Ground)

¬ At(Spare,Ground)

- S_0 consist of 5 literals (initial state and the CWA literals)
- EXPAND-GRAPH adds actions with satisfied preconditions
 - add the effects at level S₁
 - also add persistence actions and mutex relations



Repeat



Repeat until all goal literals are pairwise non-mutex in S_i

- If all goal literals are pairwise non-mutex, this means that a solution might exist
 - not guaranteed because only pairwise conflicts are checked
 - \rightarrow we need to search whether there is a solution



Deriving Heuristics from the PG

- Planning Graphs provide information about the problem
 - Example:
 - A literal that does not appear in the final level of the graph cannot be achieved by any plan
- Extraction of a serial plan
 - PG allows several actions to occur simultaneously at a level
 - can be serialized by restricting PG to one action per level
 - add mutex links between every pair of actions
 - provides a good heuristic for serial plans
- Useful for backward search
 - Any state with an unachievable precondition has cost = $+\infty$
 - Any plan that contains an unachievable precond has $cost = +\infty$
 - In general: level cost = level of first appearance of a literal
 - clearly, level cost are an admissible search heuristic
- PG may be viewed as a relaxed problem
 - checking only for consistency between pairs of actions/literals

Costs for Conjunctions of Literals

- Max-level: maximum level cost of all literals in the goal
 - admissible but not accurate
- Sum-level: sum of the level costs
 - makes the subgoal independence assumption
 - inadmissible, but works well in practice
 - Cake Example:
 - estimated costs for have (cake) \land eaten (cake) is 0+1=1
 - true costs are 2
 - Cake Example without action bake (cake)
 - estimated costs are the same
 - true costs are $+\infty$
- Set-level: find the level at which all literals appear and no pair has a mutex link
 - gives the correct estimate in both examples above
 - dominates max-level heuristic, works well with interactions

The GRAPHPLAN Algorithm

- Algorithm for extracting a solution directly from the PG
 - alternates solution extraction and graph expansion steps

```
function GRAPHPLAN(problem) returns solution or failure

graph \leftarrow INITIAL-PLANNING-GRAPH(problem)

goals \leftarrow GOALS[problem]

loop do

if goals all non-mutex in last level of graph then do

solution \leftarrow EXTRACT-SOLUTION(graph, goals,LENGTH(graph))

if solution \neq failure then return solution

else if NO-SOLUTION-POSSIBLE(graph) then return failure

graph \leftarrow EXPAND-GRAPH(graph, problem)
```

- EXTRACT-SOLUTION:
 - checks whether a plan can be found searching backwards
- EXPAND-GRAPH:
 - adds actions for the current and state literals for the next level

EXTRACT-SOLUTION

A state consists of

- a pointer to a level in the planning graph
- a set of unsatisfied goals
- Initial state
 - Iast level of PG
 - set of goals from the planning problem
- Actions
 - select any non-conflicting subset of the actions of A_{i-1} that cover the goals in the state
- Goal
 - success if level S₀ is reached with such with all goals satisfied
- Cost
 - I for each action

Could also be formulated as a Boolean CSP

- Start with goal state at (spare, axle) in S₂
 - \rightarrow only action choice is puton(spare,axle) with preconditions not(at(spare,axle)) and at(spare,ground) in S_1
 - \rightarrow two new goals in level 1



- remove (spare, trunk) is the only action to achieve at (spare, ground)
- not(at(flat,axle)) can be achieved with leave-overnight and remove(flat,axle)
- leave-overnight is mutex with remove (spare, trunk) → remove (spare, trunk) and remove (flat, axle)
- preconditions are satisfied in $S_0 \rightarrow$ we're done



Termination of GRAPHPLAN

1. The planning graph converges because everything is finite

- number of literals is monotonically increasing
 - a literal can never disappear because of the persistence actions
- number of actions is monotonically increasing
 - once an action is applicable it will always be applicable (because its preconditions will always be there)
- number of mutexes is monotonically decreasing
 - If two actions are mutex at one level, they are also mutex in all previous levels in which they appear together
 - inconsistent effects and interferences are properties of actions
 - \rightarrow if they hold once, they will always hold
 - competing needs are properties of mutexes
 - \rightarrow if the number of actions goes up, chances increase that there is a pair of non-mutex actions that achieve the preconditions
- 2. After convergence, EXTRACT-SOLUTION will find an existing solution right away or in subsequent expansions of the PG
 - more complex proof (not covered here)

SATPLAN

- Key idea:
 - translate the planning problem into propositional logic
 - similar to situation calculus, but all facts and rules are ground
 - the same literal in different situations is represented with two different propositions (we call them propositions at a depth *i*)
 - actions are also represented as propositions
 - rules are used to derive propositions of depth *i*+1 from actions and propositions of depth *i*
- Goal:
 - find a true formula consisting of propositions of the initial state, propositions of the goal state, and some action propositions
- Method:

the plan!

- use a satisfiability solver with iterative deepening on the depth
 - first try to prove the goal in depth 0 (initial state)
 - then try to prove the goal in depth 1
 - until a solution is found in depth n

Key Problem

- Complexity
 - In the worst case, a proposition has to be generated
 - for each of a actions with
 - each of o possible objects in the n arguments
 - for a solution depth d
 - \rightarrow maximum number of propositions is $d \cdot a \cdot o^n$
 - the number of rules is even larger
- Solution Attempt: Symbol Splitting
 - a possible solution is to convert each n-ary relation into n binary relations
 - "the *i*-th argument of relation *r* is *y*"
 - this will also reduce the size of the knowledge base because arguments that are not used can be omitted from the rules
 - Drawback: multiple instances of the same rule get mixed up → no two actions of same type at the same time step
- Nevertheless, SATPLAN is very competitive