## Learning

- Learning agents
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  - Different Learning Scenarios
  - Evaluation
- Neural Networks
  - Perceptrons
  - Multilayer Perceptrons
- Reinforcement Learning
  - Temporal Differences
  - Q-Learning
  - SARSA

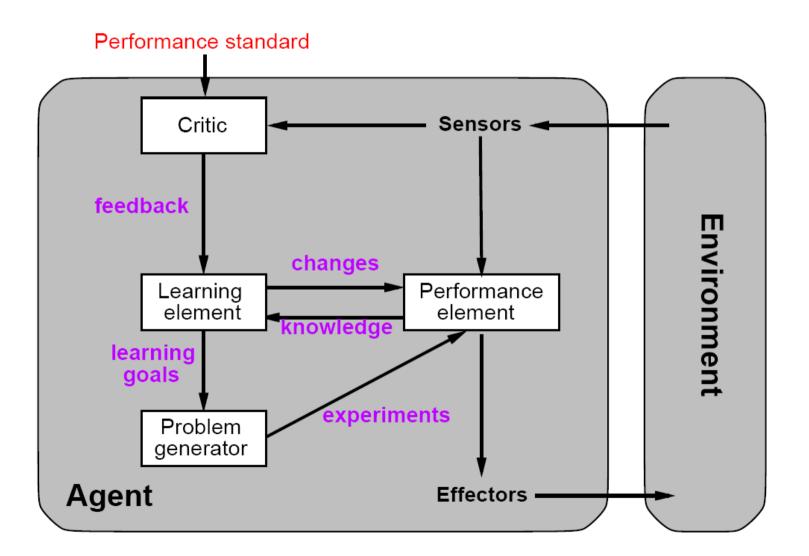
Material from Russell & Norvig, chapters 18.1, 18.2, 20.5 and 21

Slides based on Slides by Russell/Norvig, Ronald Williams, and Torsten Reil

## Learning

- Learning is essential for unknown environments,
  - i.e., when designer lacks omniscience
- Learning is useful as a system construction method,
  - i.e., expose the agent to reality rather than trying to write it down
- Learning modifies the agent's decision mechanisms to improve performance

# Learning Agents

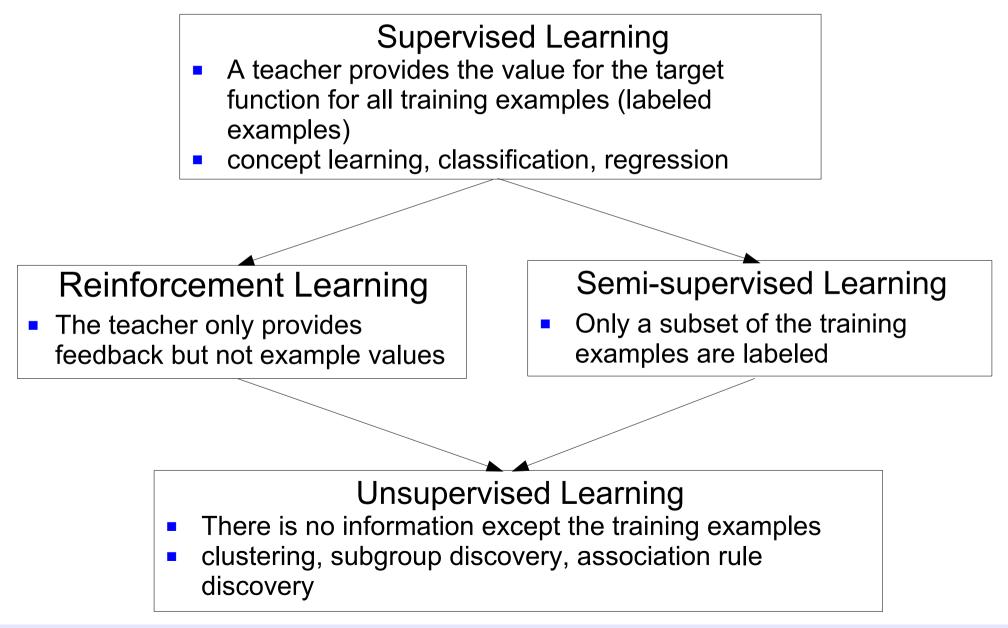


## Learning Element

Design of a learning element is affected by

- Which components of the performance element are to be learned
- What feedback is available to learn these components
- What representation is used for the components
- Type of feedback:
  - Supervised learning:
    - correct answers for each example
  - Unsupervised learning:
    - correct answers not given
  - Reinforcement learning:
    - occasional rewards for good actions

# **Different Learning Scenarios**



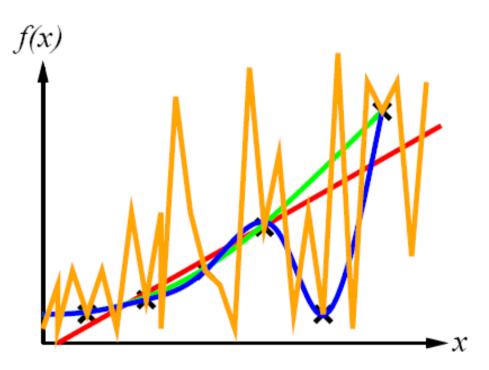
## Inductive Learning

Simplest form: learn a function from examples

- f is the (unknown) target function
- An example is a pair (x, f(x))
- Problem: find a hypothesis h
  - given a training set of examples
  - such that  $h \approx f$
  - on all examples
    - i.e. the hypothesis must generalize from the training examples
- This is a highly simplified model of real learning:
  - Ignores prior knowledge
  - Assumes examples are given

#### Inductive Learning Method

- Construct/adjust h to agree with f on training set
  - h is consistent if it agrees with f on all examples
- Example:
  - curve fitting

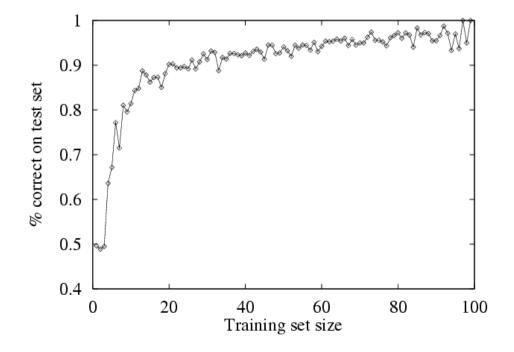


- Ockham's Razor
  - The best explanation is the simplest explanation that fits the data
- Overfitting Avoidance
  - maximize a combination of consistency and simplicity

#### **Performance Measurement**

- How do we know that  $h \approx f$ ?
  - Use theorems of computational/statistical learning theory
  - Or try h on a new test set of examples where f is known (use same distribution over example space as training set)

Learning curve = % correct on test set over training set size



## What are Neural Networks?

- Models of the brain and nervous system
- Highly parallel
  - Process information much more like the brain than a serial computer
- Learning
- Very simple principles
- Very complex behaviours
- Applications
  - As powerful problem solvers
  - As biological models

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## Pigeons as Art Experts

Famous experiment (Watanabe et al. 1995, 2001)

- Pigeon in Skinner box
- Present paintings of two different artists (e.g. Chagall / Van Gogh)
- Reward for pecking when presented a particular artist

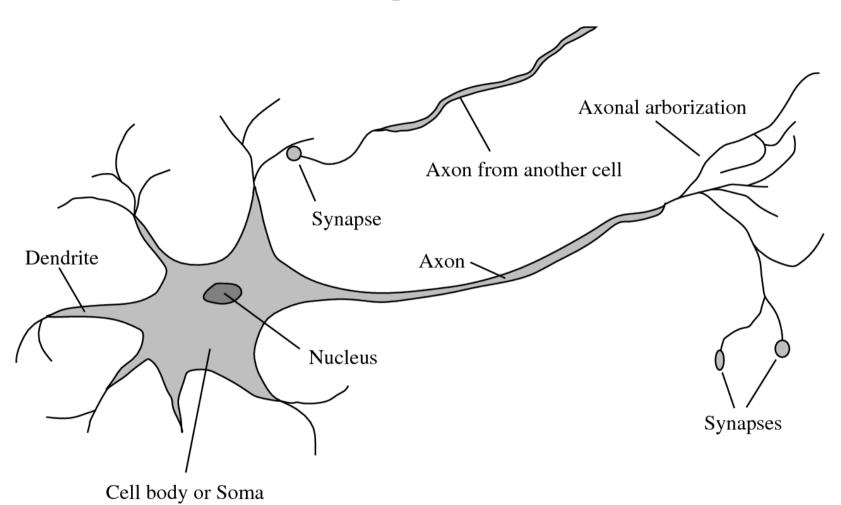




#### Results

- Pigeons were able to discriminate between Van Gogh and Chagall with 95% accuracy
  - when presented with pictures they had been trained on
- Discrimination still 85% successful for previously unseen paintings of the artists
- Pigeons do not simply memorise the pictures
- They can extract and recognise patterns (the 'style')
- They generalise from the already seen to make predictions
- This is what neural networks (biological and artificial) are good at (unlike conventional computer)

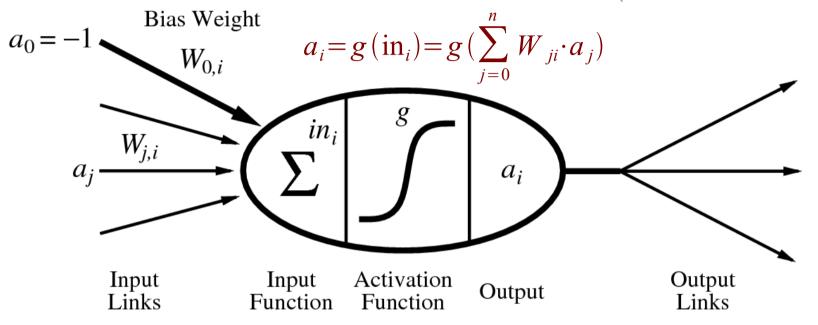
## **A Biological Neuron**



- Neurons are connected to each other via synapses
- If a neuron is activated, it spreads its activation to all connected neurons

## **An Artificial Neuron**

(McCulloch-Pitts, 1943)



- Neurons correspond to nodes or units
- A link from unit *j* to unit *i* propagates activation  $a_j$  from *j* to *i*
- The weight  $W_{j,i}$  of the link determines the strength and sign of the connection
- The total input activation is the sum of the input activations
- The output activation is determined by the activiation function g

## Perceptron

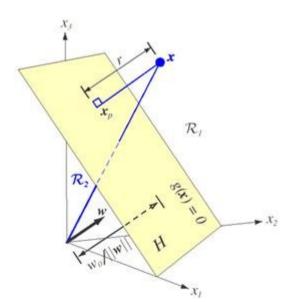
#### (Rosenblatt 1957, 1960)

- A single node
  - connecting *n* input signals  $a_i$  with one output signal *a*
  - typically signals are −1 or +1
- Activation function

• A simple threshold function:

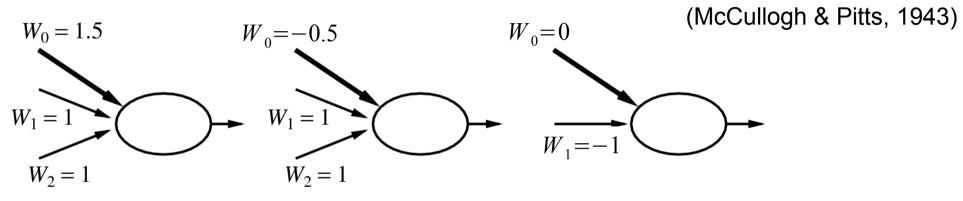
$$a = \begin{vmatrix} -1 & \text{if } \sum_{j=0}^{n} W_{j} \cdot a_{j} \le 0 \\ 1 & \text{if } \sum_{j=0}^{n} W_{j} \cdot a_{j} \ge 0 \end{vmatrix}$$

- Thus it implements a linear separator
  - i.e., a hyperplane that divides *n*-dimensional space into a region with output -1 and a region with output 1



### **Perceptrons and Boolean Fucntions**

a Perceptron can implement all elementary logical functions





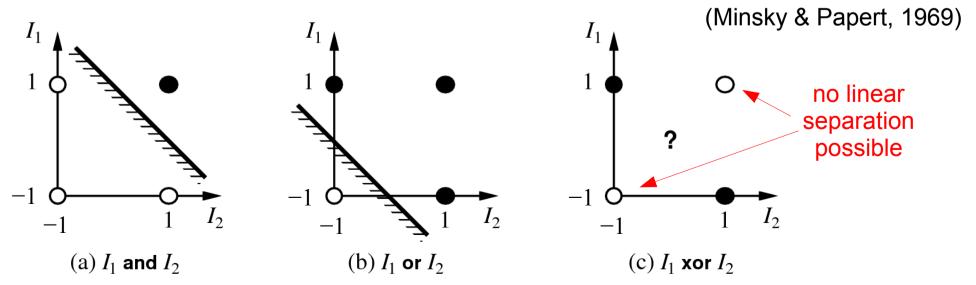




NOT

more complex functions like XOR cannot be modeled

OR



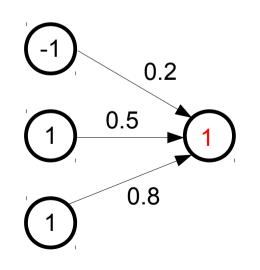
#### **Perceptron Learning**

Perceptron Learning Rule for Supervised Learning

$$W_{j} \leftarrow W_{j} + \alpha \cdot (f(\mathbf{x}) - h(\mathbf{x})) \cdot x_{j}$$

$$\downarrow$$
learning rate error

• Example:



#### Computation of output signal h(x)

in 
$$(x) = -1 \cdot 0.2 + 1 \cdot 0.5 + 1 \cdot 0.8 = 1.1$$
  
 $h(x) = 1$  because in  $(x) > 0$ 

Assume target value f(x) = -1 (and  $\alpha = 0.5$ )  $W_0 \leftarrow 0.2 + 0.5 \cdot (-1 - 1) \cdot -1 = 0.2 + 1 = 1.2$   $W_1 \leftarrow 0.5 + 0.5 \cdot (-1 - 1) \cdot 1 = 0.5 - 1 = -0.5$  $W_2 \leftarrow 0.8 + 0.5 \cdot (-1 - 1) \cdot 1 = 0.8 - 1 = -0.2$ 

Neural Networks

## Measuring the Error of a Network

- The error for one training example x can be measured by the squared error
  - the squared difference of the output value h(x) and the desired target value f(x)

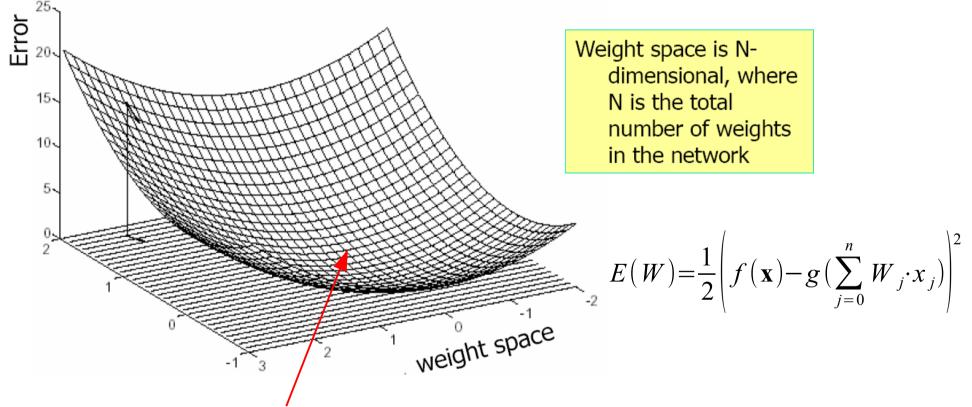
$$E(\mathbf{x}) = \frac{1}{2} Err^{2} = \frac{1}{2} (f(\mathbf{x}) - h(\mathbf{x}))^{2} = \frac{1}{2} \left| f(\mathbf{x}) - g(\sum_{j=0}^{n} W_{j} \cdot x_{j}) \right|^{2}$$

 For evaluating the performance of a network, we can try the network on a set of datapoints and average the value (= sum of squared errors)

$$E(Network) = \sum_{i=1}^{N} E(\mathbf{x}_i)$$

## **Error Landscape**

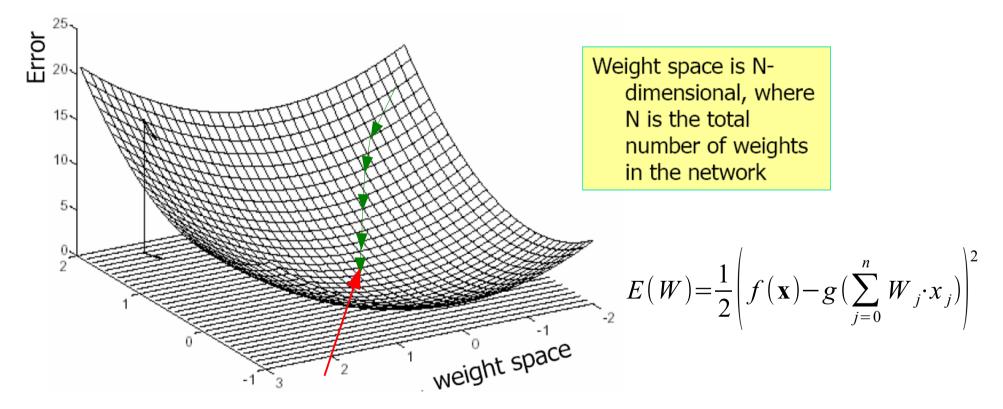
 The error function for one training example may be considered as a function in a multi-dimensional weight space



 The best weight setting for one example is where the error measure for this example is minimal

## **Error Minimization via Gradient Descent**

- In order to find the point with the minimal error:
  - go downhill in the direction where it is steepest



• ... but make small steps, or you might step over the target

# **Error Minimization**

 It is easy to derive a perceptron training algorithm that minimizes the squared error

$$E = \frac{1}{2} Err^{2} = \frac{1}{2} (f(\mathbf{x}) - h(\mathbf{x}))^{2} = \frac{1}{2} \left( f(\mathbf{x}) - g(\sum_{j=0}^{n} W_{j} \cdot x_{j}) \right)^{2}$$

 Change weights into the direction of the steepest descent of the error function

$$\frac{\partial E}{\partial W_{j}} = Err \cdot \frac{\partial Err}{\partial W_{j}} = Err \cdot \frac{\partial}{\partial W_{j}} \left( f(\mathbf{x}) - g(\sum_{k=0}^{n} W_{k} \cdot x_{k}) \right) = -Err \cdot g'(\operatorname{in}) \cdot x_{j}$$

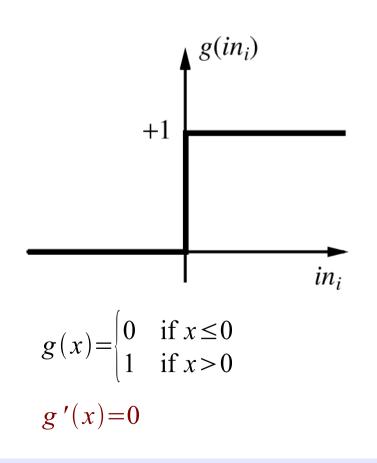
 To compute this, we need a continuous and differentiable activation function g!

• Weight update with learning rate  $\alpha$ :  $W_j = W_j + \alpha \cdot Err \cdot g'(in) \cdot x_j$ 

- positive error  $\rightarrow$  increase network output
  - increase weights of nodes with positive input
  - decrease weights of nodes with negative input

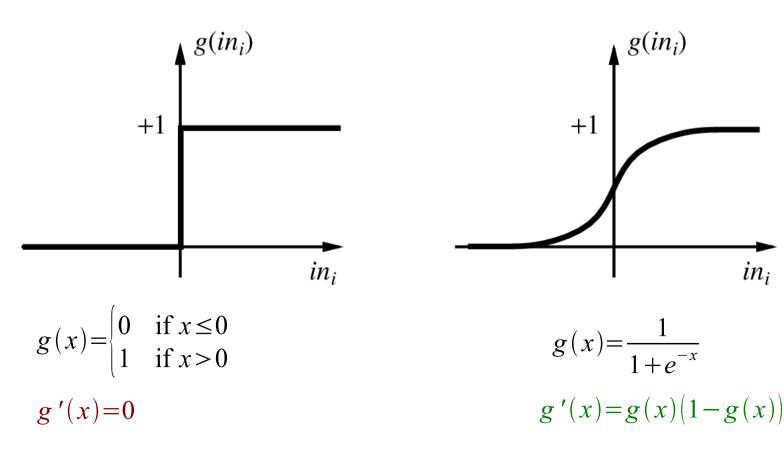
#### **Threshold Activation Function**

- The regular threshold activation function is problematic
  - g'(x) = 0, therefore  $\frac{\partial E}{\partial W_{j,i}} = -Err \cdot g'(in_i) \cdot x_j = 0$  $\rightarrow$  no weight changes!



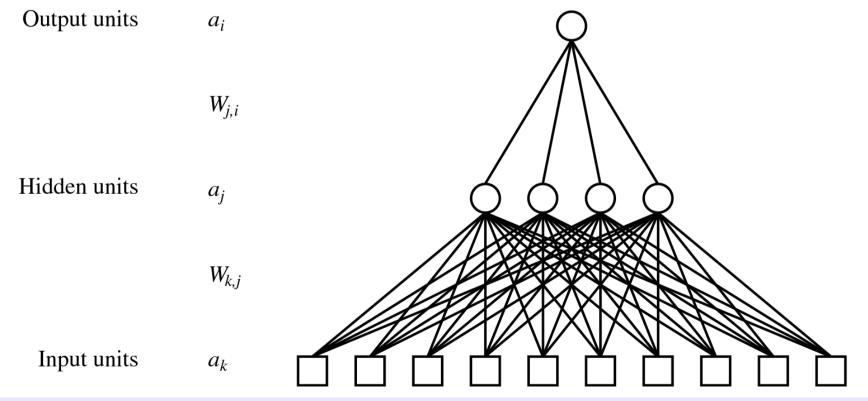
## Sigmoid Activation Function

- A commonly used activation function is the sigmoid function
  - similar to the threshold function
  - easy to differentiate
  - non-linear

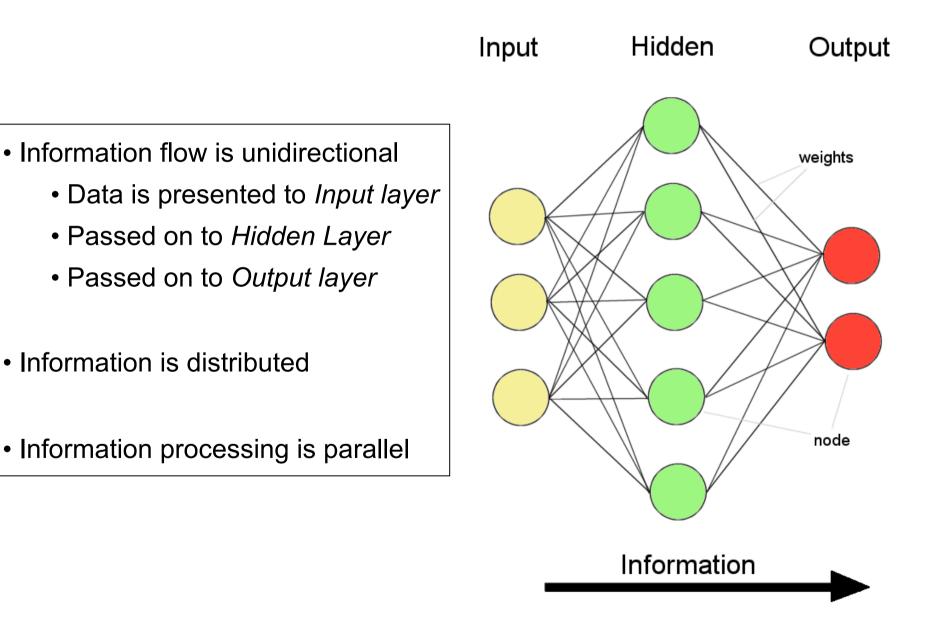


#### **Multilayer Perceptrons**

- Perceptrons may have multiple output nodes
  - may be viewed as multiple parallel perceptrons
- The output nodes may be combined with another perceptron
  - which may also have multiple output nodes
- The size of this hidden layer is determined manually



# **Multilayer Perceptrons**



#### Expressiveness of MLPs

- Every continuous function can be modeled with three layers
  - i.e., with one hidden layer
- Every function can be modeled with four layers
  - i.e., with two hidden layers

## **Backpropagation Learning**

The output nodes are trained like a normal perceptron

$$W_{ji} \leftarrow W_{ji} + \alpha \cdot Err_i \cdot g'(\operatorname{in}_i) \cdot x_j = W_{ji} + \alpha \cdot \Delta_i \cdot x_j$$

- Δ<sub>i</sub> is the error term of output node *i* times the derivation of its inputs
- the error term  $\Delta_i$  of the output layers is propagated back to the hidden layer

$$\Delta_{j} = \left(\sum_{i} W_{ji} \cdot \Delta_{i}\right) \cdot g'(\operatorname{in}_{j}) \qquad W_{kj} = W_{kj} + \alpha \cdot \Delta_{j} \cdot x_{k}$$

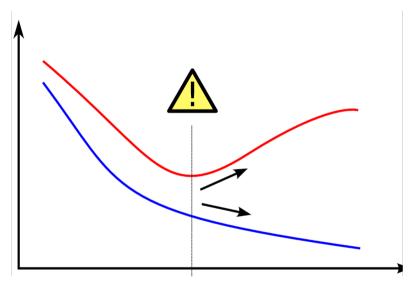
 the training signal of hidden layer node j is the weighted sum of the errors of the output nodes

#### Minimizing the Network Error

- The error landscape for the entire network may be thought of as the sum of the error functions of all examples
  - will yield many local minima  $\rightarrow$  hard to find global minimum
- Minimizing the error for one training example may destroy what has been learned for other examples
  - a good location in weight space for one example may be a bad location for another examples
- Training procedure:
  - try all examples in turn
  - make small adjustments for each example
  - repeat until convergence
- One Epoch = One iteration through all examples

## Overfitting

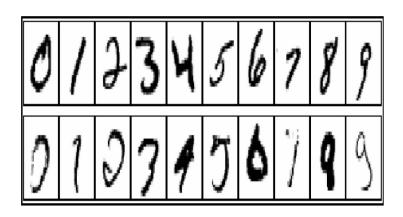
- Training Set Error continues to decrease with increasing number of training examples / number of epochs
  - an epoch is a complete pass through all training examples
- Test Set Error will start to increase because of overfitting



- Simple training protocol:
  - keep a separate validation set to watch the performance
    - validation set is different from training and test sets!
  - stop training if error on validation set gets down

# Wide Variety of Applications

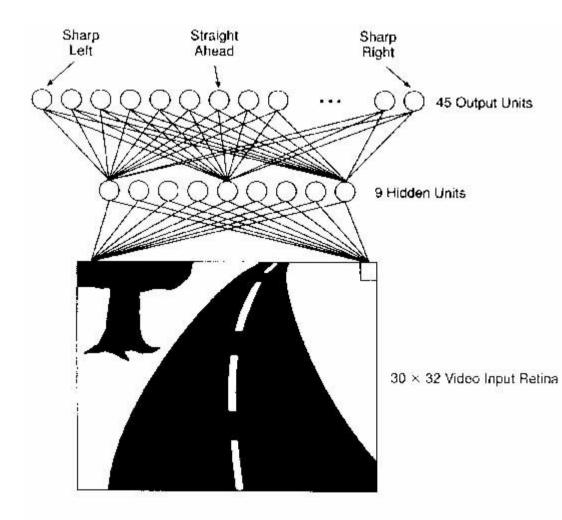
- Speech Recognition
- Autonomous Driving
- Handwritten Digit Recognition
- Credit Approval
- Backgammon
- etc.



- Good for problems where the final output depends on combinations of many input features
  - rule learning is better when only a few features are relevant
- Bad if explicit representations of the learned concept are needed
  - takes some effort to interpret the concepts that form in the hidden layers

# Autonomous Land Vehicle In a Neural Network (ALVINN)

(Dean Pomerleau)



Multilayer Network Control Unit for NavLab (From Kanade et al., 1994. © 1994 ACM. Courtesy of the authors.) Training Data: Human Driver on real roads and simulator



#### Sensory input is directly fed into the network

