Planning

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Material from Russell & Norvig, chapters 10.3. and 11

Slides based on Slides by Russell/Norvig, Lise Getoor and Tom Lenaerts

Partial-Order Planning (POP)

- **Progression and regression planning are totally ordered plan** search forms
	- this means that in all searched plans the sequence of actions is completely ordered
	- **Decisions must be made on how to sequence actions in all the** subproblems
	- \rightarrow They cannot take advantage of problem decomposition
- **If actions do not interfere with each other, they could be** made in any order (or in parallel) \rightarrow partially ordered plan
	- **if a plan for each subgoal only makes minimal commitments to** orders
		- only orders those actions that must be ordered for a successful completion of the plan
	- **it can re-order steps later on (when subplans are combined)**
	- **-** Least commitment strategy:
		- Delay choice during search

Shoe Example

Initial State: nil Goal State: RightShoe & LeftShoe


```
PRECOND: -
```

```
ADD: LeftSockOn
```

```
DELETE: -
```
)

Action(LeftShoe, PRECOND: LeftSockOn ADD: LeftShoeOn DELETE: -)

```
Action( RightSock,
PRECOND: -
ADD: RightSockOn
DELETE: -
)
```
Action(RightShoe, PRECOND: RightSockOn ADD: RightShoeOn DELETE: -)

Shoe Example

- Total-Order Planner
	- all actions are completely ordered

- Partial-Order Planner
	- **nay leave the order of** some actions undetermined
	- **any order is valid**

POP as a Search Problem

- A solution can be found by a search through Plan-Space:
	- **States are (mostly unfinished) plans**

Each plan has 4 components:

- A set of actions (steps of the plan)
- A set of ordering constraints: *A* < *B* (*A* before *B*)
	- Cycles represent contradictions.
- A set of causal links $A \rightarrow p \rightarrow B$ (*A* adds *p* for *B*)
	- The plan may not be extended by adding a new action *C* that conflicts with the causal link.
		- \blacksquare if the effect of C is \neg p and if C could come after A and before B
- A set of open preconditions
	- **Preconditions that are not achieved by action in the plan**

Example of Final Plan

- Actions = {**RightSock, RightShoe, LeftSock, LeftShoe, Start, Finish**}
- Orderings = { **RightSock < RightShoe; LeftSock < LeftShoe}**

Open preconditions $= \{ \}$

- \blacksquare Links \blacksquare { **RightSock→RightSockOn→RightShoe, LeftSock→LeftSockOn→LeftShoe, RightShoe→RightShoeOn→Finish, …**}
- **Start** Left Right Sock Sock LeftSockOn **RightSockOn** Left Right Shoe Shoe LeftShoeOn, RightShoeOn Finish

Search through Plan-Space

- **Initial State (empty plan):**
	- contains only virtual *Start* and *Finish* actions
	- ordering constraint *Start* < *Finish*
	- **no causal links**
	- all preconditions in *Finish* are open (these are the original goal)
- Successor Function (refining the plan):
	- picks one open precondition *p* on an action *B*
	- generates a successor plan for every possible *consistent* way of choosing action that achieves *p*
	- a plan is consistent iff there are no cycles in the ordering constraints and no conflicts with the causal links
- Goal test:
	- A consistent plan with no open preconditions is a solution.

Subroutines

- Refining a plan with action A, which achieves p for B:
	- add causal link $A\rightarrow p\rightarrow B$
	- add the ordering constraint *A* < *B*
	- add *Start* < *A* and *A* < *Finish* to the plan (only if *A* is new)
	- **F** resolve conflicts between
		- **new causal link and all existing actions**
		- between action *A* and all existing causal links (only if *A* is new)
- Resolving a conflict between a causal link $A\rightarrow p\rightarrow B$ and an action *C*
	- we have a conflict if the effect of C is $\neg p$ and C could come after *A* and before *B*
	- resolved by adding the ordering constraints *C* < *A* or *B* < *C*
		- both refinements are added (two successor plans) if both are consistent

Search through Plan-Space

- Operators on partial plans
	- Add an action to fulfill an open condition
	- Add a causal link
	- Order one step w.r.t another to remove possible conflicts
- Search gradually moves from incomplete/vague plans to complete/correct plans
- **Backtrack** if an open condition is unachievable or if a conflict is irresolvable
	- pick the next condition to achieve at one of the previous choice points
	- ordering of the conditions is irrelevant for completeness (the same plans will be found), but may be relevant for consistency

Executing Partially Ordered Plans

- Any particular order that is consistent with the ordering constraints is possible
	- A partial order plan is executed by repeatedly choosing any of the possible next actions.
- **This flexibility is a benefit in non-cooperative environments.**

)

)


```
Action ( remove (spare, trunk),
PRECOND: at(spare,trunk)
ADD: at(spare,ground)
DELETE: at(spare,trunk)
```
Action(leave-overnight, PRECOND: - ADD: - DELETE: at(spare,ground), at(spare,axle), at(spare,trunk), at(flat,ground), at(flat,axle))

Here we need a **not**, which is not part of the original STRIPS language!

```
Action( remove(flat,axle),
PRECOND: at(flat,axle)
ADD: at(flat,ground)
DELETE: at(flat,axle)
```

```
Action( putOn(spare,axle),
PRECOND: at(spare,ground),
       not(at(flat,axle)),
ADD: at(spare,axle)
DELETE: at(spare,ground)
)
```
- **Initial plan:**
	- Action **start** has the current state as effects
	- Action **finish** has the goal as preconditions

 $At(Spare, Axle)$ **Finish**

- Action **putOn(spare,axle)** is the only action that achieves the goal **at(spare,axle)**
- the current plan is refined to one new plan:
	- **putOn(spare,axle)** is added to the list of actions
	- add constraint **putOn(spare,axle) < finish**
	- add causal link **putOn(spare,trunk)→at(spare,axle)→finish**
	- the preconditions of **putOn(spare,trunk)** are now open

- we select the next open precondition **at(spare,ground)** as a goal
- only **at(spare,ground)** can achieve this goal
- the current plan is refined to a new one as before

- we select the next open precondition **not(at(flat,axle))** as a goal
- could be achieved with two actions
	- **leave-overnight**
	- **remove(flat,axle)**
	- \rightarrow we have two successor plans

Plan 1: **leave-overnight**

- is in conflict with the constraint **remove(spare,trunk)→remove(spare,trunk)→putOn(spare,axle)** \rightarrow has to be ordered before remove (spare, trunk)
- the condition **at(spare,trunk)** has to be achieved next
	- **start** is the only action that can achive this
	- however, **start** is in conflict with **leave-overnight**
	- \blacksquare this conflict cannot be resolved \rightarrow backtracking

Plan 2: **remove(flat,axle)**

- achieves goal **not(at(flat,axle))**
- corresponding causal link and order relation are added
- **at(flat,axle)** becomes open precondition

- open precondition **at(spare,trunk)**is selected as goal
	- action **start** is added
	- corresponding causal link and order relation are added

- open precondition **at(spare,trunk)**is selected as goal
	- action **start** is added
	- corresponding causal link and order relation are added
- open precondition **at(flat,axle)**is selected as goal
	- action **start** is added
	- corresponding causal link and order relation are added
- no more open preconditions remain
	- \rightarrow plan is completed

POP in First-Order Logic

- **Operators may leave some** variables unbound
- **Example**
	- Achieve goal **on(a,b)** with action **move(a,From,b)**
	- **It remains unspecified from** where block **a** should be moved (**PRECOND: on(a,From)**)

```
Action( move(Block,From,To),
PRECOND: on(Block,From),
          clear(Block),
          clear(To),
ADD: on(Block,To),
          clear(From),
DELETE: on(Block,From),
          clear(To)
)
```
• Two approaches

- Decide for one binding and backtrack later on (if necessary)
- Defer the choice for later (least commitment)
- **Problems with least commitment:**
	- e.g., an action that has **on(a,From)**on its delete-list will only conflict with above if both are bound to the same variable
	- can be resolved by introducing inequality constraint.

Heuristics for Plan-Space Planning

- Not as well understood as heuristics for state-space planning
- General heuristic: number of distinct open preconditions
	- maybe minus those that match the initial state
	- underestimates costs when several actions are needed to achieve a condition
	- overestimates costs when multiple goals may be achieved with a single action
- Choosing a good precondition to refine has also a strong impact
	- select open condition that can be satisfied in the fewest number of ways
		- analogous to most-constrained variable heuristic from CSP
	- **Two important special cases:**
		- select a condition that cannot be achieved at all (early failure!)
		- select deterministic conditions that can only be achived in one way

Planning Graph

- A planning graph is a special structure used to
	- **E** achieve better heuristic estimates.
	- directly extract a solution using GRAPHPLAN algorithm
- Consists of a sequence of levels (time steps in the plan)
	- **Level 0 is the initial state.**
- Each level consists of a set of literals and a set of actions.
	- **Literals = all those that could be true at that time step**
		- depending upon the actions executed at the preceding time step
	- Actions = all those actions that could have their preconditions satisfied at that time step
		- depending on which of the literals actually hold.
	- Only a restricted subset of possible negative interactions among actions is recorded
- **Planning graphs work only for propositional problems**
	- STRIPS and ADL can be propositionalized

- Initial state: **have(cake)**
- Goal state: **have(cake), eaten(cake)**

```
Action( eat(cake),
PRECOND: have(cake)
ADD: eaten(cake)
DELETE: have(cake)
)
```

```
Action( bake(cake),
PRECOND: not(have(cake))
ADD: have(cake)
DELETE: -
)
```
Persistence Actions

- pseudo-actions for which the effect equals the precondition
- **analogous to frame axioms**
- **are automatically added by** the planner

Mutual exclusions

 \blacksquare link actions or preconditions that are mutually exclusive (*mutex*)

 \blacksquare Start at level \mathcal{S}_0 , determine action level \mathcal{A}_0 and next level \mathcal{S}_1

- A_0 contains all actions whose preconditions are satisfied in the previous level S₀
- Connect preconditions and effects of these actions
- Inaction is represented by persistence actions
- **Level** A_0 contains the actions that could occur
	- Conflicts between actions are represented by mutex links

- **Per construction, Level** $S₁$ **contains all literals that could** result from picking any subset of actions in A_0
	- Conflicts between literals that can not occur together are represented by mutex links.
	- *S*¹ defines multiple states and the mutex links are the constraints that define this set of states
- Continue until two consecutive levels are identical
	- Or contain the same amount of literals (explanation later)

Mutex Relations

- A mutex relation holds between two actions when:
	- **Inconsistent effects:**
		- one action negates the effect of another.
	- **Interference:**
		- one of the effects of one action is the negation of a precondition of the other
	- Competing needs:
		- one of the preconditions of one action is mutually exclusive with the precondition of the other.
- A mutex relation holds between two literals when:
	- **Inconsistent support:**
		- If one is the negation of the other OR
		- **if each possible action pair that could achieve the literals is** mutex

Deriving Heuristics from the PG

- **Planning Graphs provide information about the problem**
	- Example:
		- A literal that does not appear in the final level of the graph cannot be achieved by any plan
- Useful for backward search
	- Any state with an unachievable precondition has cost = $+\infty$
	- Any plan that contains an unachievable precond has cost = $+\infty$
	- In general: level cost = level of first appearance of a literal
		- clearly, level cost are an admissible search heuristic
- **Serial Plan Graph**
	- **PG allows several actions to occur simultaneously at a level**
	- can be serialized by restricting PG to one action per level
		- **add mutex links between every pair of actions**
	- **Perovides a better heuristic for serial plans**
- **PG may be viewed a relaxed problem**
	- checking only for consistency between pairs of actions/literals

Costs for Conjunctions of Literals

- Max-level: maximum of the goal
	- **admissible but not accurate**
- **Sum-level:** sum of the level costs
	- **makes the subgoal independence assumption**
	- **inadmissible, but works well in practice**
	- Cake Example:
		- estimated costs for **have(cake)** ∧ **eaten(cake)** is 0+1=1
		- \blacksquare true costs are 2
	- Cake Example without action **bake(cake)**
		- **Exercise is estiamted costs are the same**
		- true costs are +∞
- Set-level: find the level at which all literals appear and no pair has a mutex link
	- gives the correct estimate in both examples above
	- dominates max-level heuristic, works well with interactions

The GRAPHPLAN Algorithm

- Algorithm for extracting a solution directly from the PG
	- alternates solution extraction and graph expansion steps

```
function GRAPHPLAN(problem) returns solution or failure
  graph ← INITIAL-PLANNING-GRAPH(problem)
  goals ← GOALS[problem]
  loop do
       if goals all non-mutex in last level of graph then do
           solution ← EXTRACT-SOLUTION(graph, goals,LENGTH(graph))
          if solution \neq failure then return solution
           else if NO-SOLUTION-POSSIBLE(graph) then return failure
          graph ← EXPAND-GRAPH(graph, problem)
```
- EXTRACT-SOLUTION:
	- checks whether a plan can be found searching backwards
- **EXPAND-GRAPH:**
	- adds actions for the current and state literals for the next level

$S₀$ consist of 5 literals (initial state and the CWA literals)

At(Flat, Axle)

 \neg At(Spare, Axle)

□At(Flat, Ground)

 \neg At(Spare, Ground)

- $S₀$ consist of 5 literals (initial state and the CWA literals)
- EXPAND-GRAPH adds actions with satisfied preconditions
	- add the effects at level S₁
	- also add persistence actions and mutex relations

■ Repeat

Repeat until all goal literals are pairwise non-mutex in *S*ⁱ

Solution might exist and EXTRACT-SOLUTION will try to find it

EXTRACT-SOLUTION

A state consists of

- a pointer to a level in the planning graph
- a set of unsatisfied goals
- **F** Initial state
	- **last level of PG**
	- **set of goals from the planning problem**
- Actions
	- select any set of non-conflicting subset of the actions of *A*i-1 that cover the goals in the state
- Goal
	- $\textcolor{red}{\bullet}$ success if level $\textsf{S}_{\textup{0}}$ is reached with such with all goals satisfied
- Cost
	- **1** for each action

Could also be formulated as a Boolean CSP

- Start with goal state \mathbf{a} t (spare, \mathbf{axle}) in \mathcal{S}_2
- only action choice is **puton(spare,axle)** with preconditions **not(at(spare,axle))** and **at(spare,ground)** in *S*¹
- **E** leave-overnight is mutex with remove (spare, trunk) **→ remove(spare,trunk)** and **remove(flat,axle)**
- **preconditions are satisfied in** $S_0 \rightarrow$ **we're done**

Termination of GRAPHPLAN

- 1. The planning graph converges because everything is finite
	- **number of literals is monotonically increasing**
		- a literal can never disappear because of the persistence actions
	- number of actions is monotonically increasing
		- **once an action is applicable it will always be applicable** (because its preconditions will always be there)
	- **number of mutexes is monotonically decreasing for a fixed set** of literals
		- more precisely: If two actions are mutex at one level, they are also mutex in all previous levels in which they appear together
		- **· inconsistent effects and interferences are properties of actions**
		- \rightarrow if they hold once, they will always hold
		- competing needs are properties of mutexes
		- \rightarrow if the number of actions goes up, chances in crease that there is a pair of non-mutex actions that achieve the preconditions
- 2. It can also be shown that EXTRACT-SOLUTION will find a solution in one of the subsequent expansions of the PG

SATPLAN

- Key idea:
	- **translate the planning problem into propositional logic**
	- similar to situation calculus, but all facts and rules are ground
		- the same literal in different situations is represented with two different propositions (we call them propositions at a depth *i*)
	- **EXECTE:** actions are also represented as propositions
	- \blacksquare rules are used to derive propositions of depth $i+1$ from actions and propositions of depth *i*
- Goal:
	- find a true formula consisting of propositions of the initial state, propositions of the goal state, and some action propositions
- Method:

the plan!

- use a satisfiability solver with iterative deepening on the depth
	- first try to prove the goal in depth 0 (initial state)
	- then try to prove the goal in depth 1
	- until a solution is found in depth *n*

Key Problem

- **Complexity**
	- I In the worst case, a proposition has to be generated
		- \blacksquare for each of a actions with
		- each of *o* possible objects in the *n* arguments
		- **for a solution depth d**
	- → maximum number of propositions is $d \cdot a \cdot o^n$
	- the number of rules is even larger
- Solution Attempt: Symbol Splitting
	- a possible solution is to convert each n-ary relation into n binary relation
		- \blacksquare "the *i*-th argument of relation r is y "
	- **this will also reduce the size of the knowledge base because** arguments that are not used can be omitted from the rules
	- Drawback: multiple instances of the same rule get mixed up \rightarrow no two actions of same type at the same time step
- **Nevertheless, SATPLAN is very competitive**