Learning

- Learning agents
- Inductive learning
  - Different Learning Scenarios
  - Evaluation
- Neural Networks
  - Perceptrons
  - Multilayer Perceptrons
- Reinforcement Learning
  - Temporal Differences
  - Q-Learning
  - SARSA

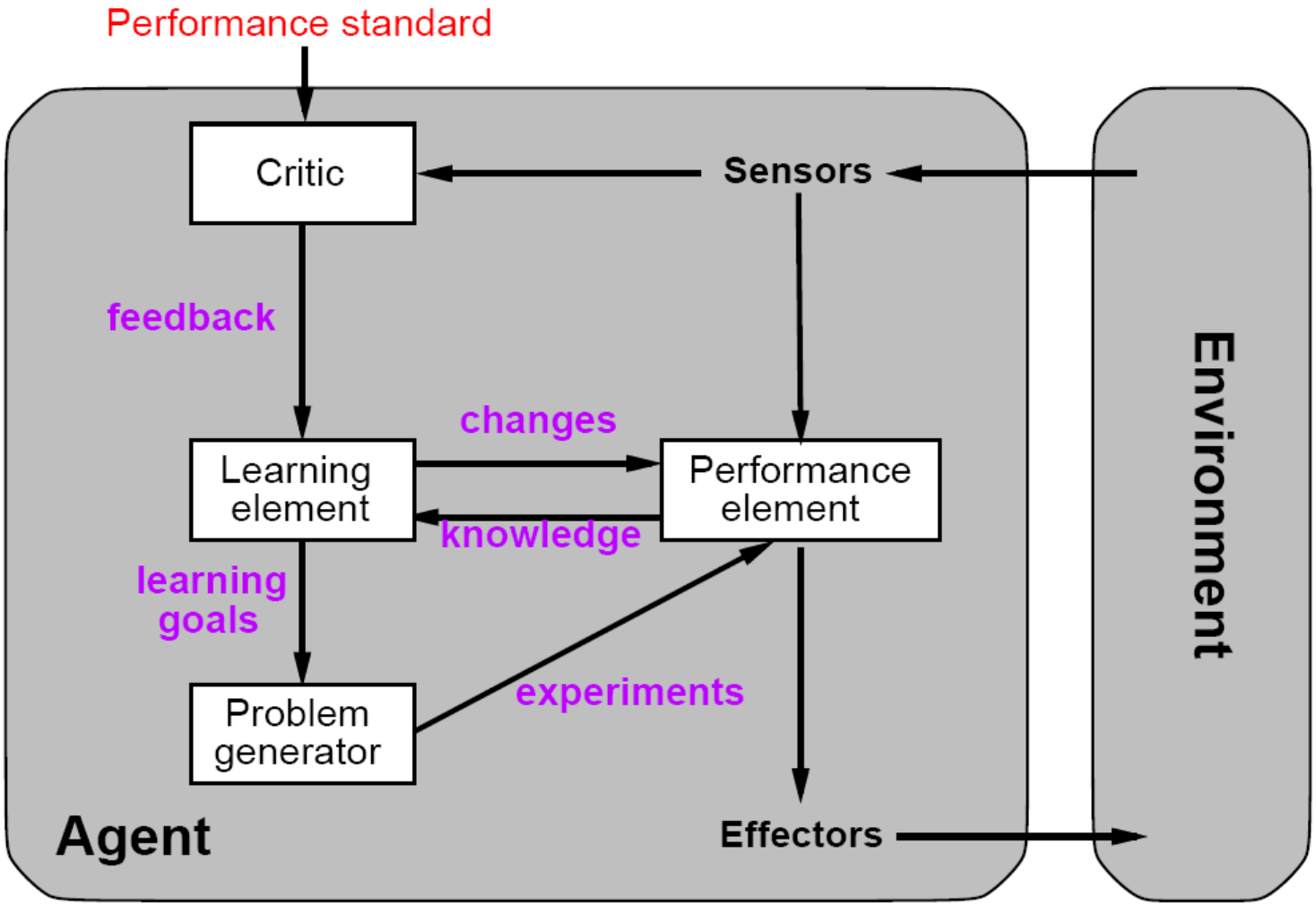
Material from Russell & Norvig, chapters 18.1, 18.2, 20.5 and 21

Slides based on Slides by Russell/Norvig, and Torsten Reil

Learning

- Learning is essential for unknown environments,
  - i.e., when designer lacks omniscience
- Learning is useful as a system construction method,
  - i.e., expose the agent to reality rather than trying to write it down
- Learning modifies the agent's decision mechanisms to improve performance

Learning Agents



Learning Element

- Design of a learning element is affected by
  - Which components of the performance element are to be learned
  - What feedback is available to learn these components
  - What representation is used for the components
- Type of feedback:
  - Supervised learning: correct answers for each example
  - Unsupervised learning: correct answers not given
  - Reinforcement learning: occasional rewards

Different Learning Scenarios

Supervised Learning

- A teacher provides the value for the target function for all training examples (labeled examples)
- concept learning, classification, regression

Reinforcement Learning

- The teacher only provides feedback but not example values

Semi-supervised Learning

- Only a subset of the training examples are labeled

Unsupervised Learning

- There is no information except the training examples
- clustering, subgroup discovery, association rule discovery

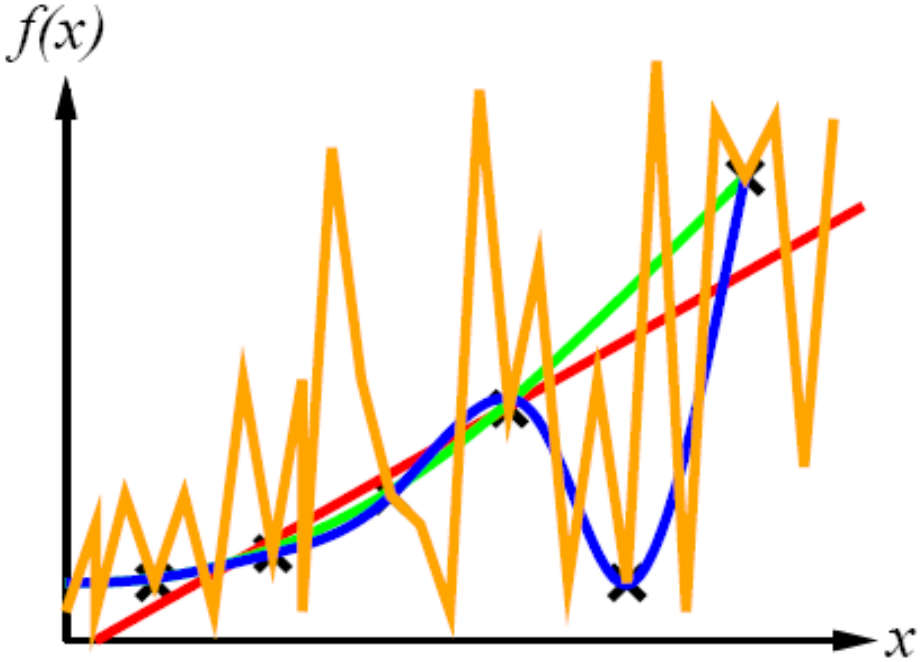
Inductive Learning

Simplest form: learn a function from examples

- f is the target function
- An example is a pair $(x, f(x))$
- Problem: find a hypothesis h
  such that $h \approx f$
  given a training set of examples
- This is a highly simplified model of real learning:
  - Ignores prior knowledge
  - Assumes examples are given

Inductive Learning Method

- Construct/adjust h to agree with f on training set
  (h is consistent if it agrees with f on all examples)
- Example:
  - curve fitting

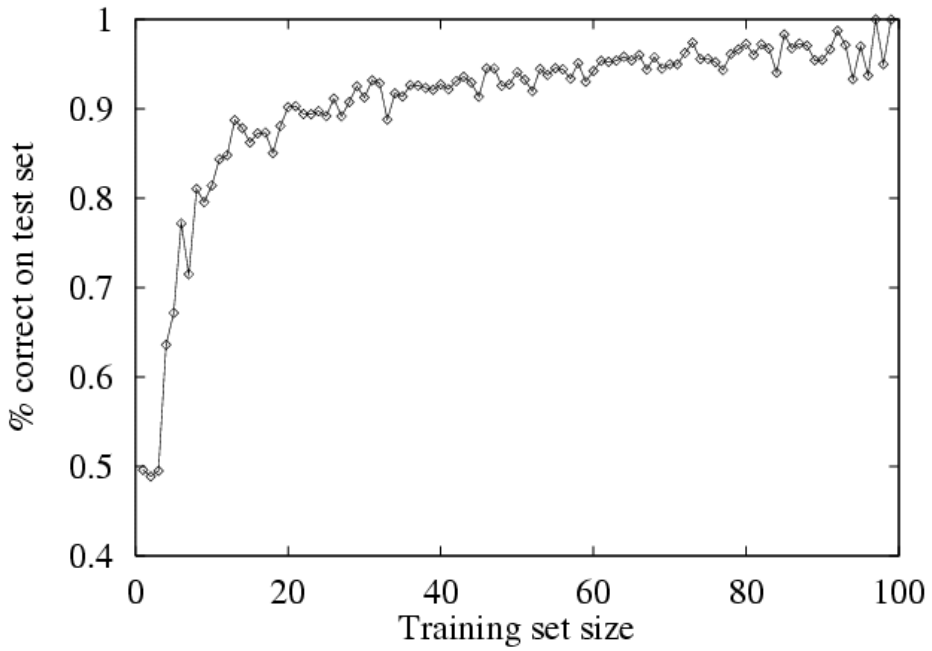


- Ockham's Razor
  - The best explanation is the simplest explanation that fits the data
- Overfitting Avoidance
  - maximize a combination of consistency and simplicity

Performance Measurement

- How do we know that $h \approx f$?
  - Use theorems of computational/statistical learning theory
  - Try h on a new test set of examples where f is known (use same distribution over example space as training set)

Learning curve = % correct on test set over training set size



What are Neural Networks?

- Models of the brain and nervous system
- Highly parallel
  - Process information much more like the brain than a serial computer
- Learning

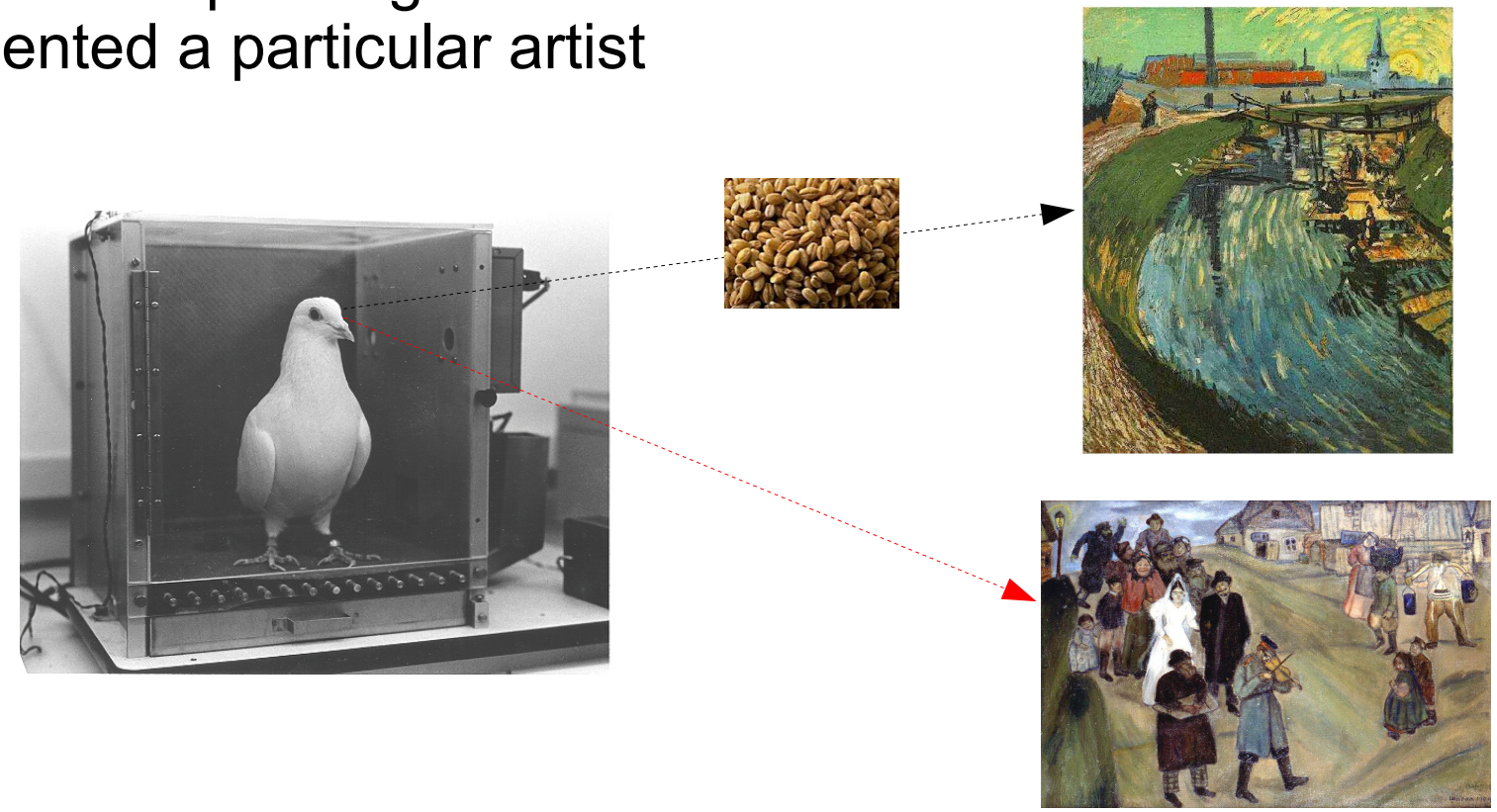
- Very simple principles
- Very complex behaviours

- Applications
  - As powerful problem solvers
  - As biological models

Pigeons as Art Experts

Famous experiment (Watanabe *et al.* 1995, 2001)

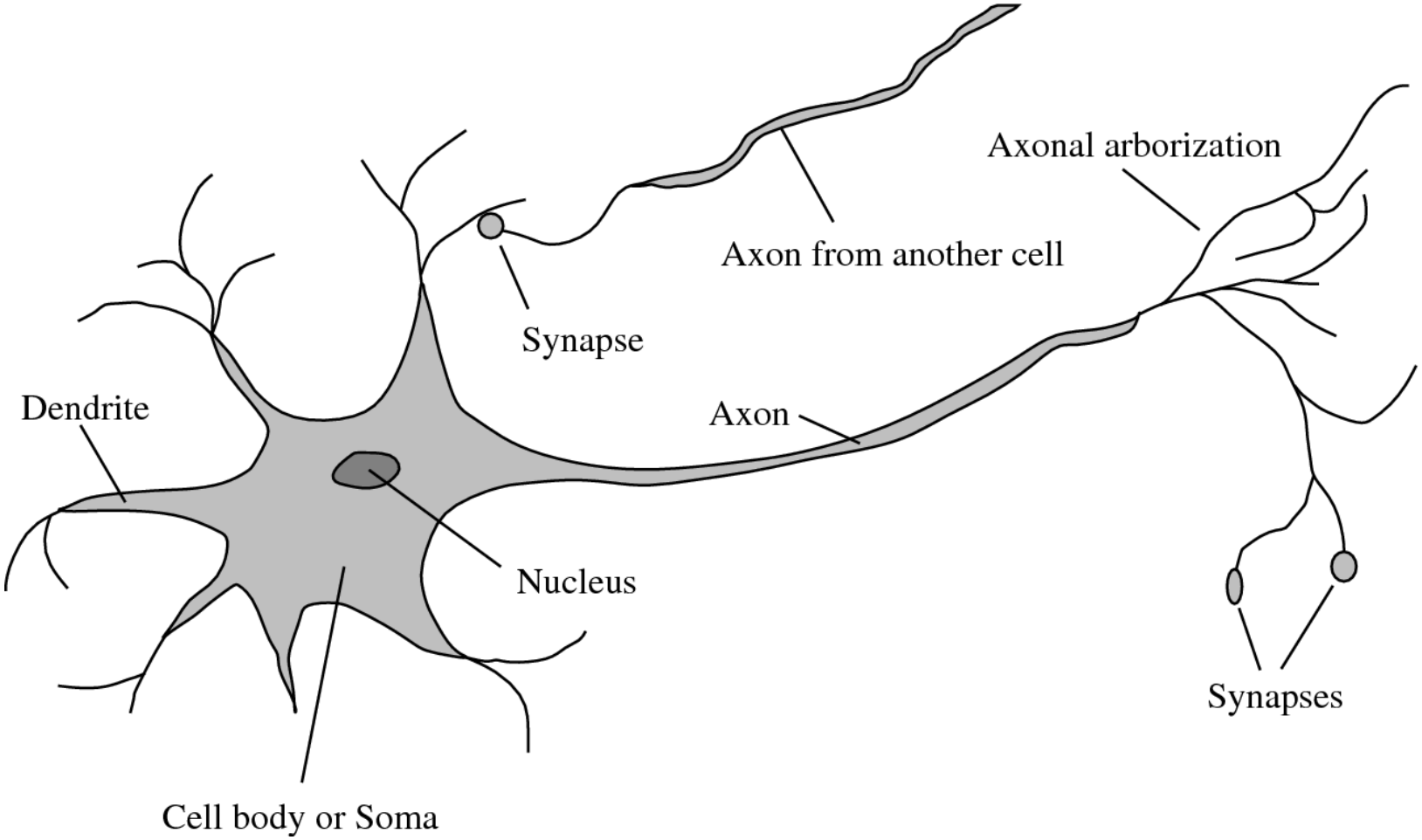
- Pigeon in Skinner box
- Present paintings of two different artists (e.g. Chagall / Van Gogh)
- Reward for pecking when presented a particular artist



Results

- Pigeons were able to discriminate between Van Gogh and Chagall with 95% accuracy (when presented with pictures they had been trained on)
- Discrimination still 85% successful for previously unseen paintings of the artists
- Pigeons do not simply memorise the pictures
- They can extract and recognise patterns (the ‘style’)
- They generalise from the already seen to make predictions
- This is what neural networks (biological and artificial) are good at (unlike conventional computer)

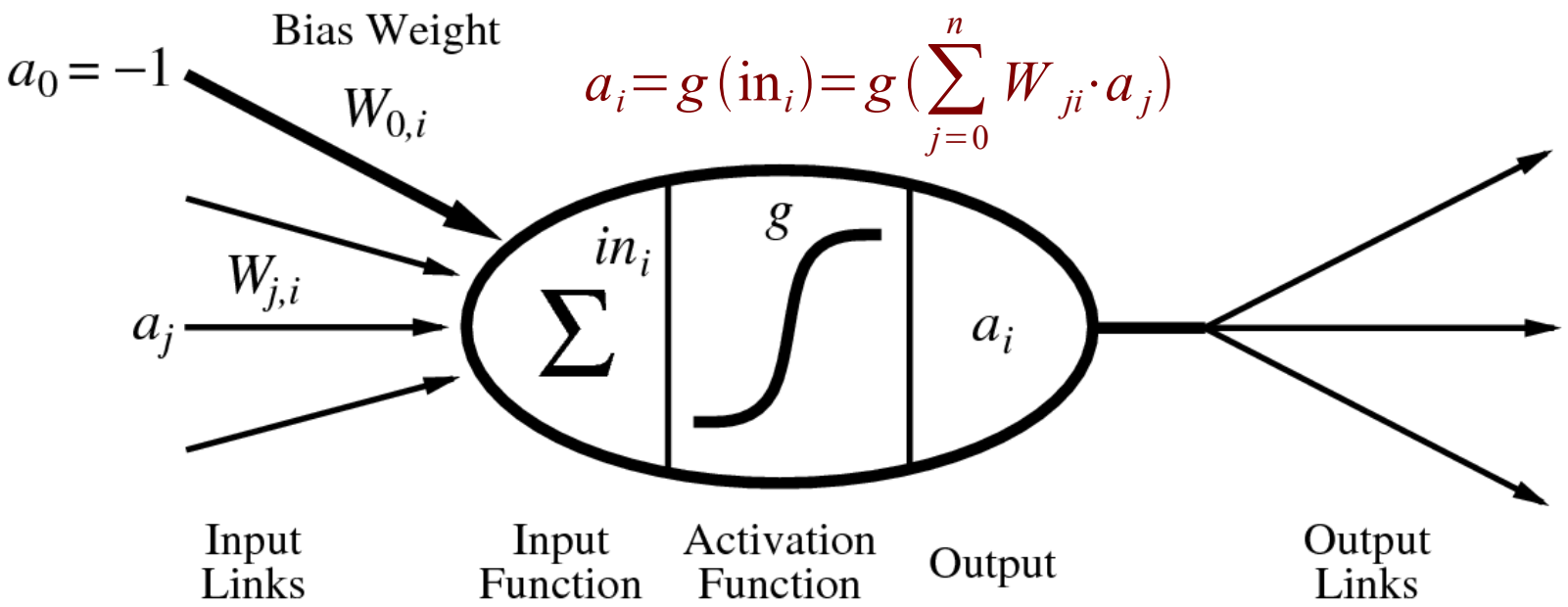
A Biological Neuron



- Neurons are connected to each other via synapses
- If a neuron is activated, it spreads its activation to all connected neurons

An Artificial Neuron

(McCulloch-Pitts,1943)



- Neurons correspond to nodes or units
- A link from unit i to unit j propagates activation a_j from j to i
- The weight $W_{i,j}$ of the link determines the strength and sign of the connection
- The total input activation is the sum of the input activations
- The output activation is determined by the activiation function g

Perceptron

(Rosenblatt 1957, 1960)

- A single node
  - connecting n input signals with one output signal

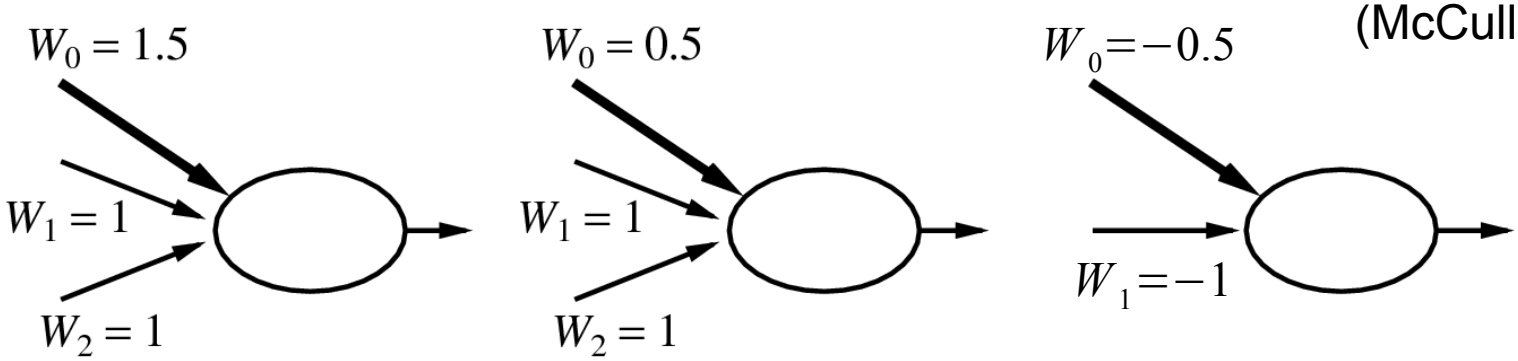
- Activation function
  - A simple threshold function: $a_i = \begin{cases} -1 & \text{if } \sum_{i=0}^{n} W_{ij} \cdot a_j \leq 0 \\ 1 & \text{if } \sum_{i=0}^{n} W_{ij} \cdot a_j > 0 \end{cases}$

- Thus it implements a linear separator
  - i.e., a hyperplane that divides n-dimensional space into a region with output 0 and a region with output 1

Perceptrons and Boolean Fucntions

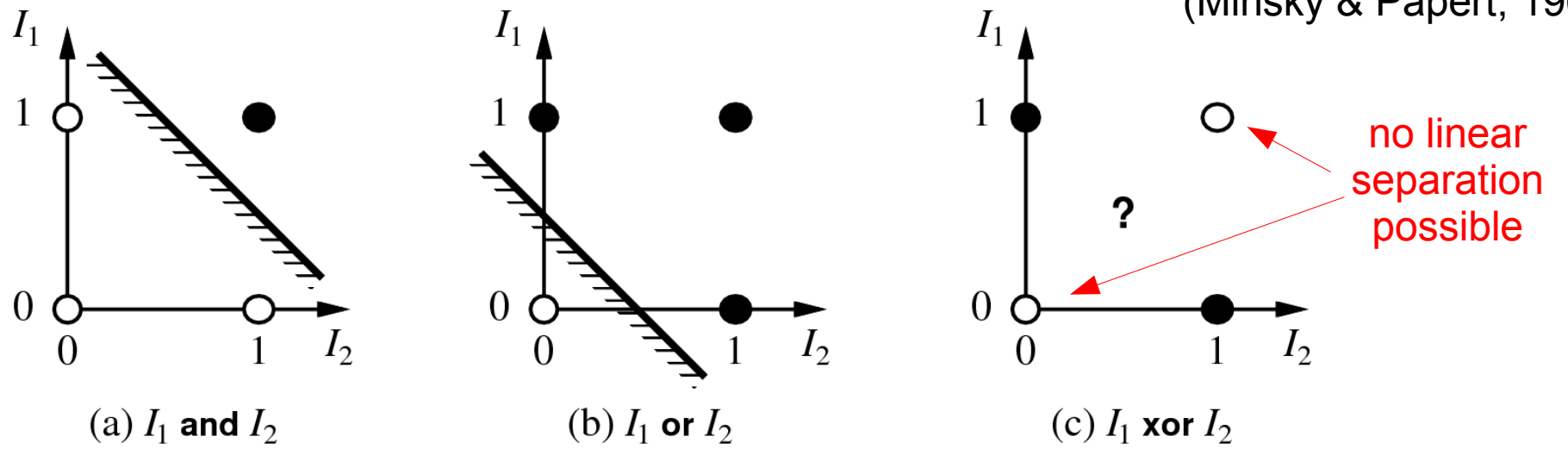
- a Perceptron can implement all elementary logical functions

(McCullogh & Pitts, 1943)



- more complex functions like XOR cannot be modeled

(Minsky & Papert, 1969)



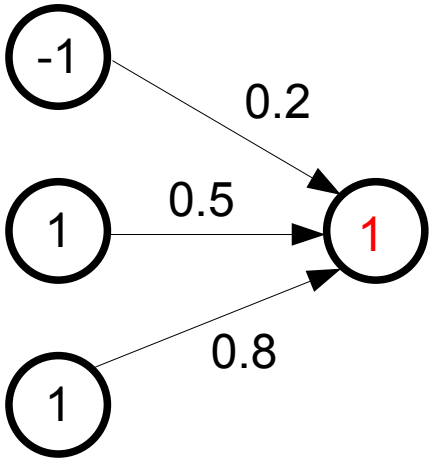
Perceptron Learning

- Perceptron Learning Rule for Supervised Learning

$$W_i \leftarrow W_i + \alpha \cdot (f(\mathbf{x}) - h(\mathbf{x})) \cdot x_i$$

learning rate — error

- Example:



Computation of output signal $h(x)$

$$\text{in}(x) = -1 \cdot 0.2 + 1 \cdot 0.5 + 1 \cdot 0.8 = 1.1$$

$$h(x) = 1 \text{ because } \text{in}(x) > 0$$

Assume target value $f(x) = -1$ (and $\alpha = 0.5$)

$$W_0 \leftarrow 0.2 + 0.5 \cdot (-1 - 1) \cdot -1 = 0.2 + 1 = 1.2$$

$$W_1 \leftarrow 0.5 + 0.5 \cdot (-1 - 1) \cdot 1 = 0.5 - 1 = -0.5$$

$$W_2 \leftarrow 0.8 + 0.5 \cdot (-1 - 1) \cdot 1 = 0.8 - 1 = -0.2$$

Error Minimization

- It is easy to derive a perceptron training algorithm that minimizes the squared error

$$E = \frac{1}{2} Err^2 = \frac{1}{2}(f(\mathbf{x}) - h(\mathbf{x}))^2 = \frac{1}{2}\left(f(\mathbf{x}) - g(\sum_{i=0}^{n} W_j \cdot x_j)\right)^2$$

- Change weights into the direction of the steepest descent of the error function

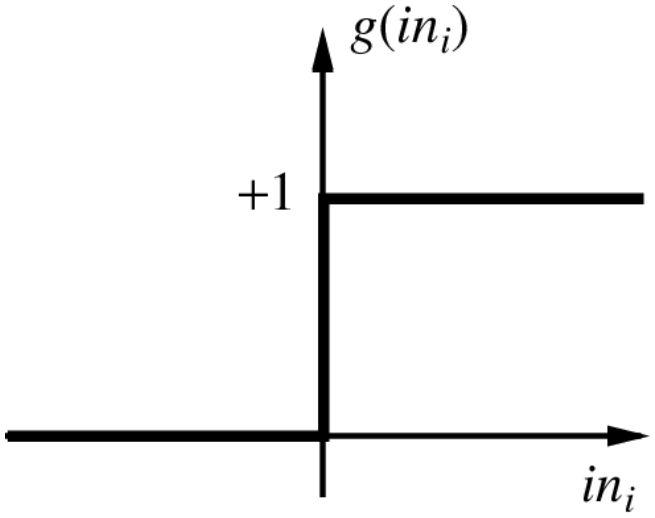
$$\frac{\partial E}{\partial W_j} = Err \cdot \frac{\partial Err}{\partial W_j} = Err \cdot \frac{\partial}{\partial W_j}\left(f(\mathbf{x}) - g(\sum_{i=0}^{n} W_j \cdot x_j)\right) = -Err \cdot g'(\text{in}) \cdot x_j$$

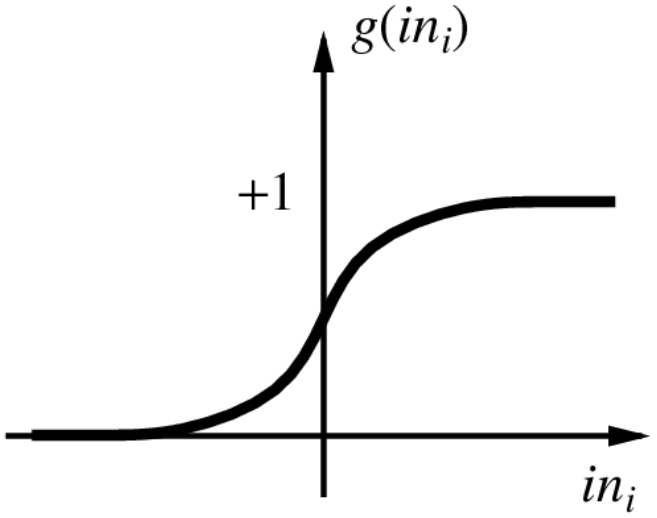
  - To compute this, we need a continuous and differentiable activation function g!

- Weight update with learning rate α: $W_j = W_j + \alpha \cdot Err \cdot g'(\text{in}) \cdot x_j$
  - positive error → increase network output
    - increase weights of nodes with positive input
    - decrease weights of nodes with negative input

Sigmoid Activation Function

- A commonly used activation function is the sigmoid function
  - similar to the threshold function
  - easy to differentiate
  - non-linear



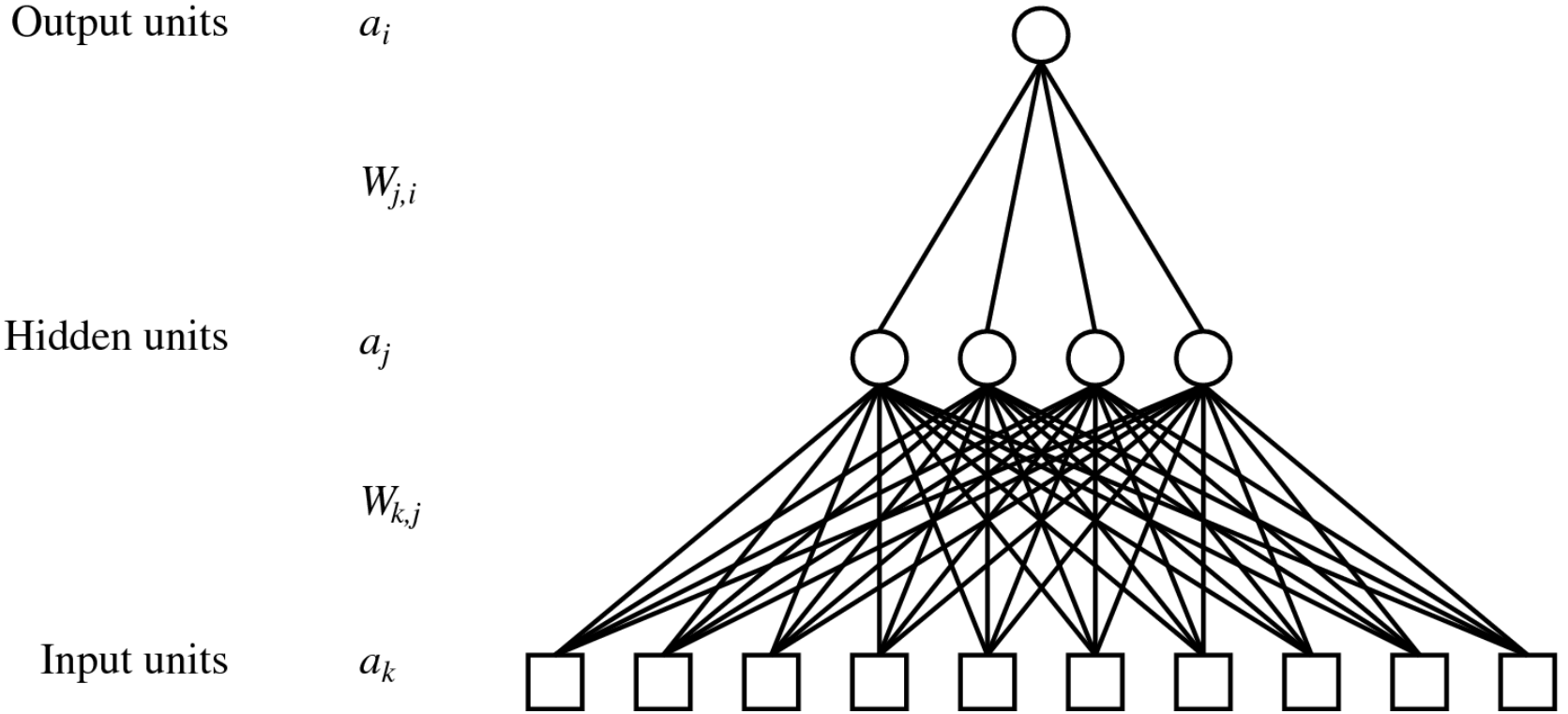


$$g(x) = \frac{1}{1+e^{-x}}$$

$$g'(x) = g(x)\left(1 - g(x)\right)$$

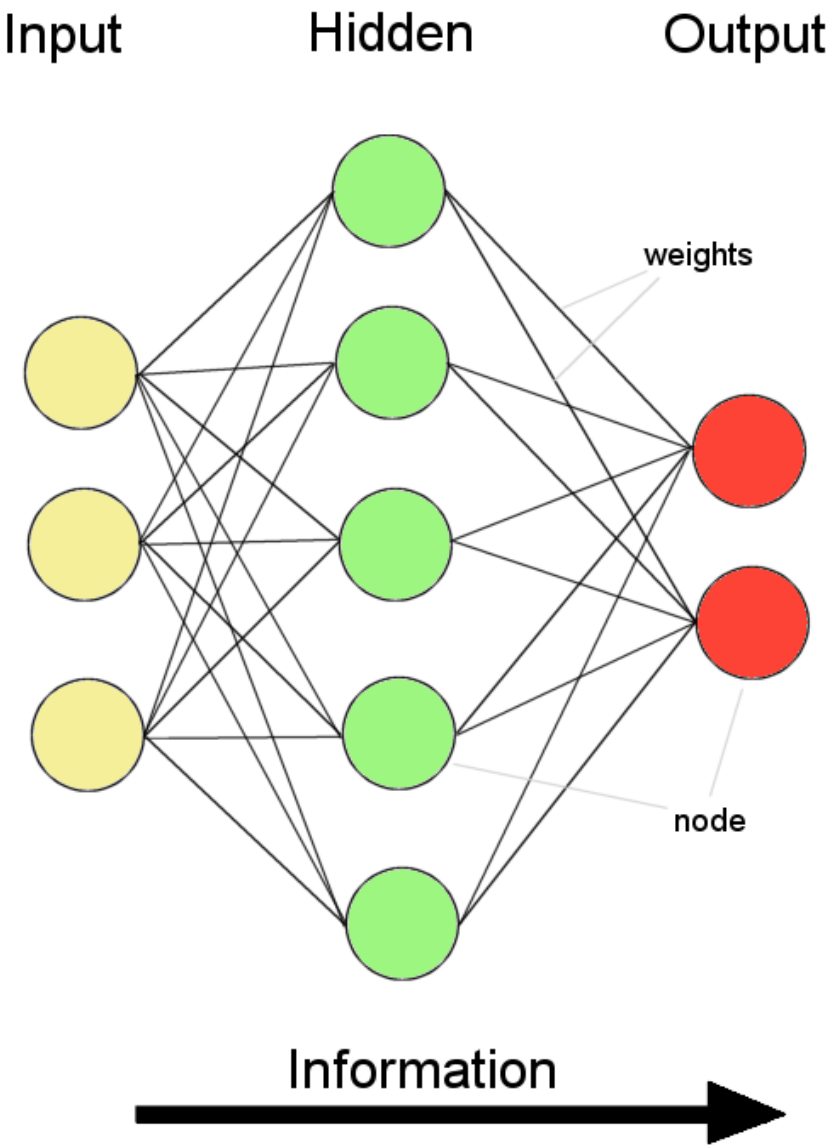
Multilayer Perceptrons

- Perceptrons may have multiple output nodes
  - may be viewed as multiple parallel perceptrons
- The output nodes may be combined with another perceptron
  - which may also have multiple output nodes
- The size of this hidden layer is determined manually



Multilayer Perceptrons

- Information flow is unidirectional
  - Data is presented to *Input layer*
  - Passed on to *Hidden Layer*
  - Passed on to *Output layer*
- Information is distributed
- Information processing is parallel



Expressiveness of MLPs

- Every continuous function can be modeled with two layers
- Every function with three layers

Backpropagation Learning

- The output nodes are trained like a normal perceptron

$$W_{ji} = W_{ji} + \alpha \cdot Err_i \cdot g'(\text{in}_i) \cdot x_j = W_{ji} + \alpha \cdot \Delta_i \cdot x_j$$

  - Δ_i is the error of output node i times the derivation of its inputs

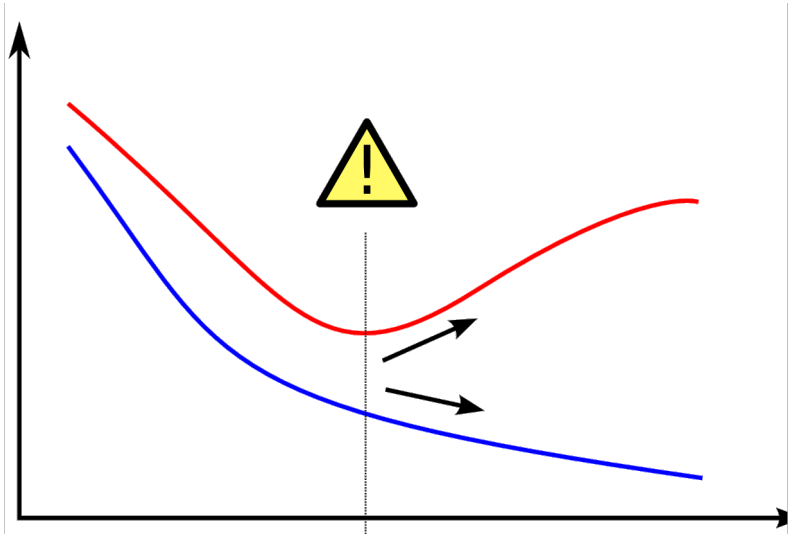
- the error of the output layers back to the hidden layer

$$\Delta_j = \left(\sum_i W_{ji} \cdot \Delta_i \right) \cdot g'(\text{in}_j) \qquad W_{kj} = W_{kj} + \alpha \cdot \Delta_j \cdot x_k$$

  - the training signal of hidden layer node j is the weighted sum of the errors of the output nodes

Overfitting

- Training Set Error continues to decrease with increasing number of training examples / number of epochs
  - an epoch is a complete pass through all training examples
- Test Set Error will start to increase because of overfitting



- Simple training protocol:
  - keep a separate validation set to watch the performance
    - validation set is different from training and test sets!
  - stop training if error on validation set gets down